RANDOM DIFFERENTIAL TOPOLOGY

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In my Phd thesis [1] I developed some general methods to study the topological and geometric properties of random smooth maps. This topic is at the crossroad of Differential Topology and Probability.

In this talk, I will present such methods by studying the expected topology of singular sets of random (Kostlan) polynomials, when the degree grows to infinity [3].

This involves a generalization of the Kac-Rice formula [2], a probabilistic version of Thom transversality theorem [4], a Morse inequality for stratified manifolds [3] and a deterministic result on the behavior of Betti numbers under continuous perturbations [3].

This is a joint work with Antonio Lerario.

References

[1] STECCONI M., Random Differential Topology, arXiv, Ph.D. thesis, 2020.

- [2] STECCONI M., Kac-Rice formula for transverse intersections, Analysis and Mathematical Physics, vol. 12, 2022.
- [3] LERARIO A. AND STECCONI M., Maximal and Typical Topology of Real Polynomial Singularities, Annales de L'Institut Fourier, to appear, 2019.
- [4] LERARIO A. AND STECCONI M., Differential Topology of Gaussian Random Fields, arXiv, 2019.